

# Applications in Engineering with the Help of the TI-92

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## DC Analysis

### Example A:

We want to compute the electrical currents in the DC-circuit shown below:

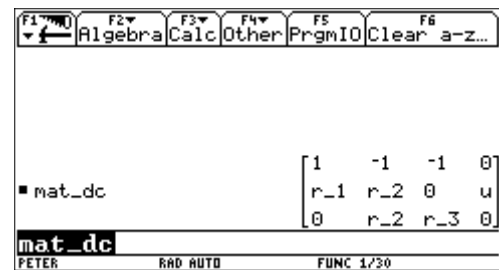
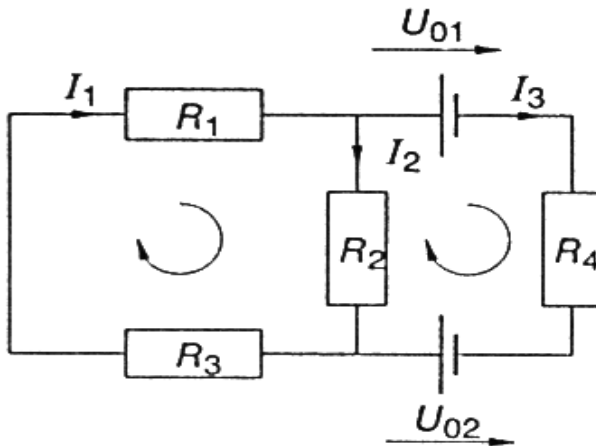


Figure 1

We have the following equations:

- 1)  $I_1 - I_2 - I_3 = 0$
- 2)  $R_1 \cdot I_1 + R_2 \cdot I_2 = U$
- 3)  $R_2 \cdot I_2 - R_3 \cdot I_3 = 0$

We use the DATA/MATRIX EDITOR to store this matrix: ( see Figure 1 )

- 1)  $1 \quad -1 \quad -1 \quad 0$
- 2)  $R_1 \quad R_2 \quad 0 \quad U \Rightarrow \text{mat\_dc}$
- 3)  $0 \quad R_2 \quad -R_3 \quad 0$

We use the rref-command to get the results:

$\text{rref}(\text{mat\_dc}) \Rightarrow$

The results  $I_1, I_2$  and  $I_3$  can be seen in the right column of Figure 2:

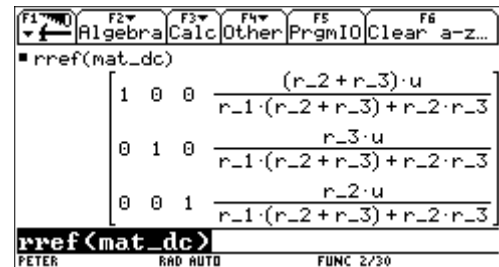
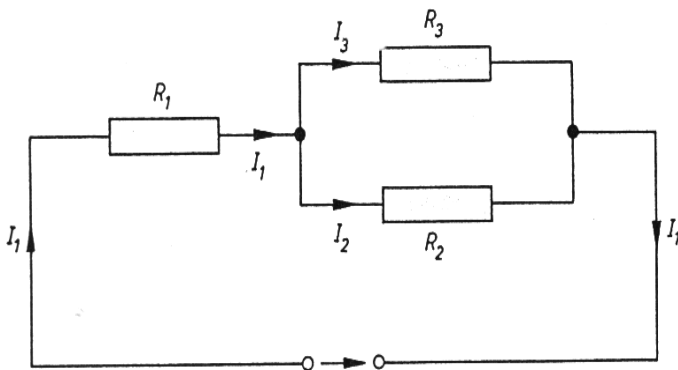


Figure 2

Now we want to compute a numerical example:

### Example B:



We get the corresponding equation system:

- 1)  $I_1 - I_2 - I_3 = 0$
- 2)  $20 \cdot I_1 + 30 \cdot I_2 + 25 \cdot I_3 = 0$
- 3)  $-30 \cdot I_2 + 15 \cdot I_3 = 20$

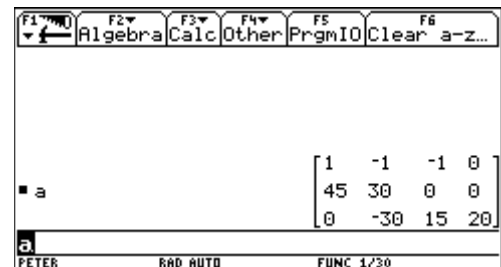


Figure 3

This time we store the data under the name a ( see Figure 3 ) :

We can compute the results very easily using the rref-command:

You can see the results in the fourth column of the matrix: ( see figure 4 )

$$\begin{aligned} I_1 &= .24 \text{ A} \\ I_2 &= -.36 \text{ A} \\ I_3 &= .61 \text{ A} \end{aligned}$$

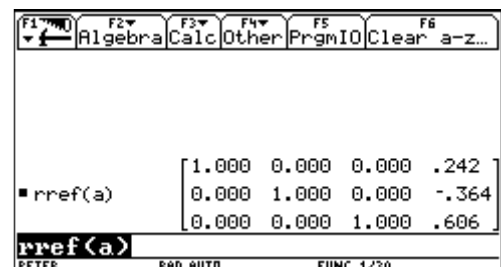


Figure 4

**Example C:**

Now we will compute the forces  $F_A$  and  $F_B$  of a supporting beam: ( see Figure 5 )

With  $F_1 = 300$  N

$F_2 = 250$  N

$\alpha = 40^\circ$

$l_1 = 0.7$  m

$l_2 = 0.4$  m

$l_3 = 0.3$  m

We get the following equation system:

$$1) F_A + F_{BY} - F_1 - F_2 \cdot \sin(\alpha) = 0$$

$$2) F_{BX} - F_2 \cdot \cos(\alpha) = 0$$

$$3) -F_1 \cdot l_1 - F_2 \cdot \sin(\alpha) \cdot (l_1 + l_2) + F_{BY} \cdot (l_1 + l_2 + l_3) = 0$$

$$1) F_A + F_{BY} = 300 + 250 \cdot \sin(40^\circ)$$

$$2) F_{BX} = 250 \cdot \cos(40^\circ)$$

$$3) 1.4 F_{BY} = 300 \cdot 0.7 + 250 \cdot 1.1 \cdot \sin(40^\circ)$$

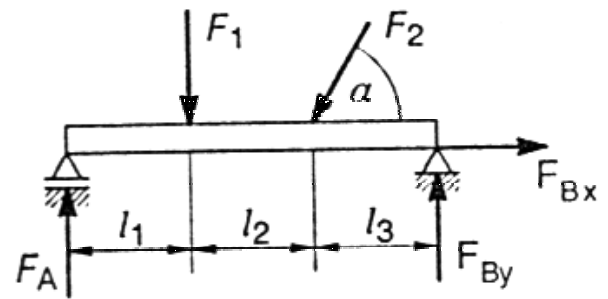


Figure 5

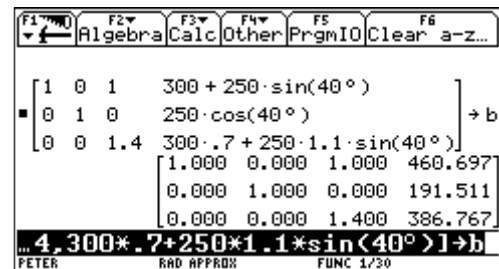


Figure 6

By using the rref-command we get the following solution:

$F_A = 184.44$  N

$F_{BX} = 191.51$  N

$F_{BY} = 276.26$  N

since

$$F_B = \sqrt{F_{BX}^2 + F_{BY}^2}$$

thus we get

$F_B = 336.15$  N

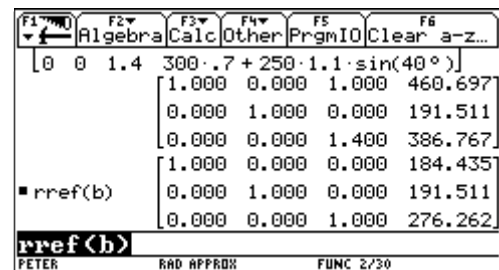


Figure 7

## Cycloids ( Rollcurves )

Rollcurves are created by a circle rolling on a straight line or on another circle (without sliding ). They have been developed in mechanical engineering with the investigation of cog wheels.

### Example A: Cycloids

develop if a circle rolls on a straight line.

( without sliding ):

We change the type of the FUNCTION to PARAMETRIC.

The formula of the regular cycloid is given by

$$x_t = r * ( t - a * \sin ( t ) ) \quad \text{and} \\ y_t = r * ( 1 - a * \cos ( t ) ).$$

We choose  $r = 4$  and  $a = 1$  to get the **regular form**. ( Figure 8 ). We watch the path of a point on the circumference of the rolling circle.

For figure 9 we set  $a = .6$  to get the **stretched form** of the cycloid. This curve develops if we watch a point inside the rolling circle

We set  $a = 2$  ( see figure 10 ) to get the **intricated form** of the cycloid. This form develops if the point we watch lies on the lengthened radius of the rolling circle.

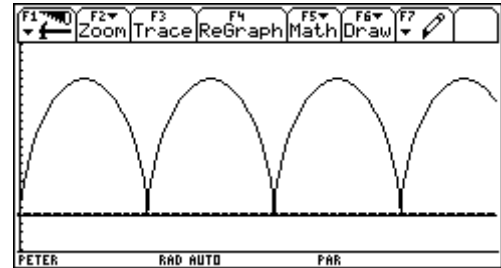


Figure 8

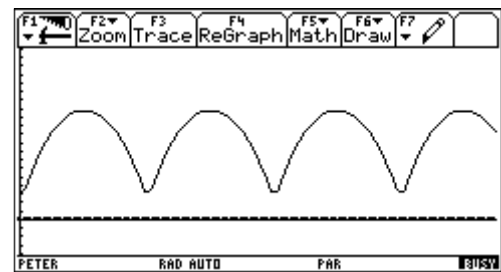


Figure 9

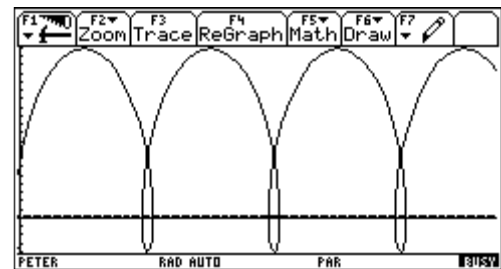


Figure 10

## Example B: Epicycloids

These curves develop if a small circle rolls on a large circle.

We change the mode of the graph from FUNCTION to PARAMETRIC.

The formula of an epicycloid consists of two equations: (see figure 11 ).

$$x_t = (r_1 + r_2) \cos(t) - r_2 \cdot \cos\left(\frac{r_1 + r_2}{r_2} t\right)$$

$$y_t = (r_1 + r_2) \sin(t) - r_2 \cdot \sin\left(\frac{r_1 + r_2}{r_2} t\right)$$

with  $r_1$  is the radius of the large circle and  
 $r_2$  is the radius of the small circle.

If you choose both radii in that way that their ratio is integer, then the curve is symmetric and closed.

We choose  $r_1 = 4$  and  $r_2 = 1$  to get the **regular form** of the curve: (see figure 12).

We use ZOOMSQR to get equal distances on both axes.

Now we are searching for the **stretched form** of the curve. We change the factor of the second term to  $.6 < r_2$

That means we watch a point inside the small circle by the movement.

Now the curve is not in contact with the circle.  
 ( See figure 13 ).

Now we change the factor of the second term to  $2 > r_2$ . That means we watch a point on the lengthened radius of the smaller circle by the movement.

In this case we get the **intricated form** of the curve (see figure 14 ).

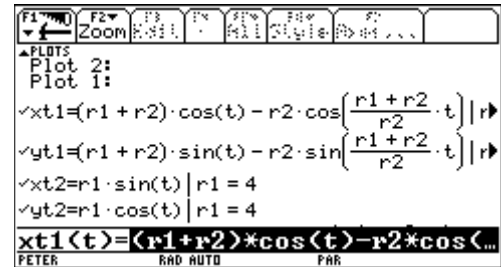


Figure 11

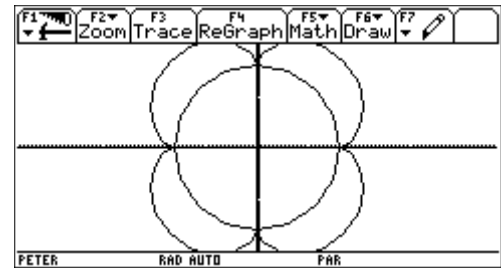


Figure 12

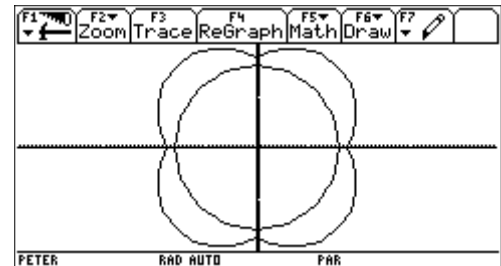


Figure 13

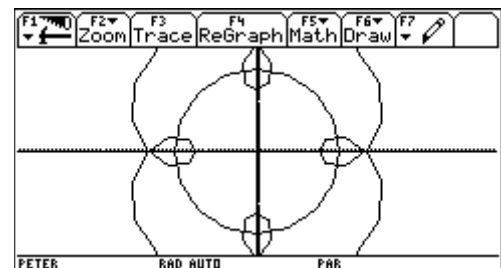


Figure 14

### Example C: Hypocycloids

develop if a small circle rolls inside a larger circle.

The formula of a hypocycloid in parametric form is: (see figure 15):

$$x_t = (r_1 - r_2) \cos(t) + r_2 \cdot \cos((r_1 - r_2)/r_2)t$$

$$y_t = (r_1 - r_2) \sin(t) + r_2 \cdot \sin((r_1 - r_2)/r_2)t$$

with  $r_1$  is the radius of the large circle and

$r_2$  is the radius of the small circle.

With  $r_1 = 5$  and  $r_2 = 1$  we get the **regular form**

of the curve: (see figure 16).

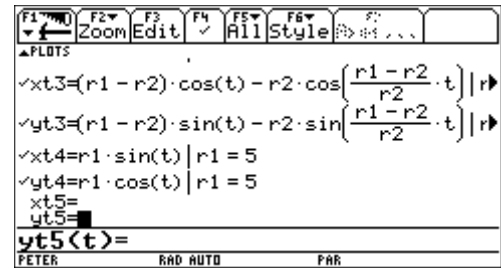


Figure 15

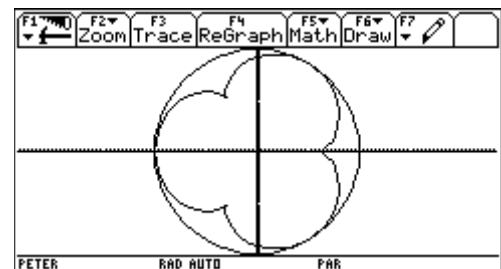


Figure 16

Now we are searching for the **stretched form**

of the curve. We change the factor of the second term to  $.6 < r_2$

This means that we watch a point inside the small circle by the movement.

Now the curve doesn't contact the circle.

(see figure 17).

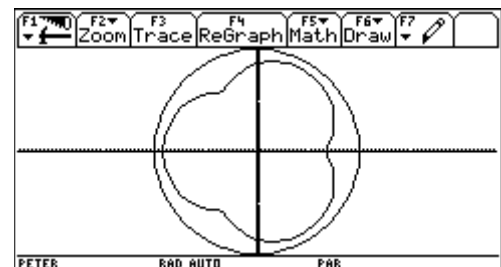


Figure 17

Then we change the factor of the second

term to  $2 > r_2$

We watch a point on the lengthened radius of the smaller circle by the movement.

In this case we get the **intricated form**

( see figure 18 ).

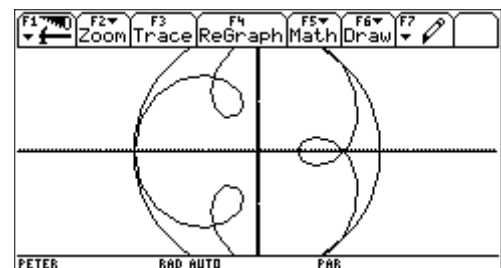


Figure 18

## Lissajous figures

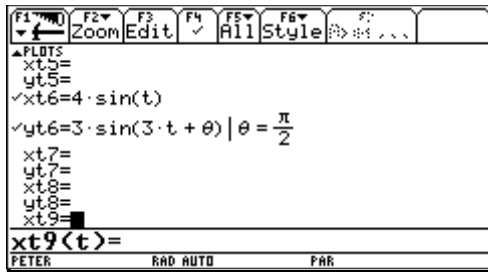
Lissajous figures develop, if two vertical oscillations superimpose each other.

In parametric form we have:

$$x_t = 4 \cdot \sin(t)$$

$$y_t = 3 \cdot \sin(3t + \varphi) \quad \text{with } \varphi = \pi/2, \pi/4, 3\pi/4 \text{ respectively ( see figure 19 ).}$$

Figure 19



The reader is encouraged to experiment on his own. See figures 20,21,22 for example.

## Beats

Beats are oscillations with a periodically increasing and decreasing amplitude. They are created by the superposition of two harmonic oscillations:

We can write the formula as a product of sinus and cosinus functions with different periods.  
Let us investigate the following curves:

$$y_1 = 2 \cdot \cos(x) \cdot \sin(19x) \quad (\text{ see figure 23 })$$

$$Y_2 = 3 \cdot \cos(99x) \cdot \sin(x) \quad (\text{ see figure 24 })$$

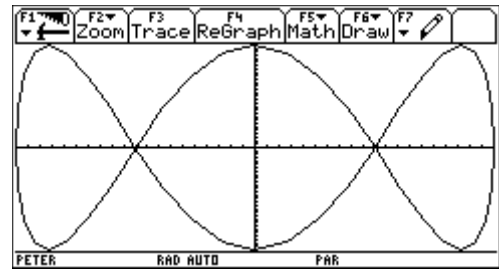


Figure 20

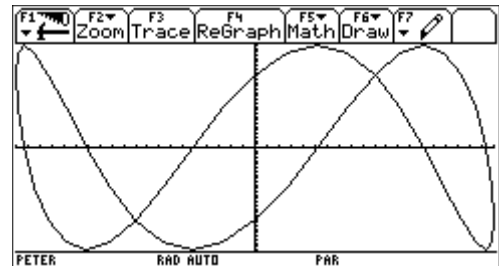


Figure 21

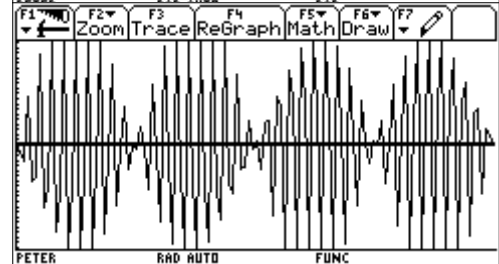
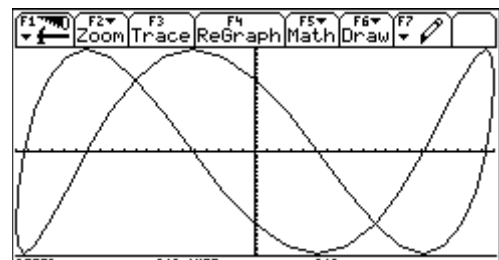


Figure 22

Figure 23

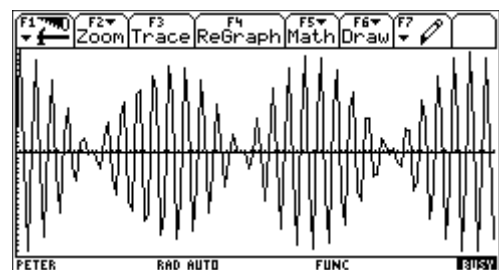


Figure 24

## Fourier Analysis

In electrical engineering any oscillations can be built up by sinus and cosinus functions.

We will describe the most important examples. We change MODE to FUNCTION and use a trigonometric window.

### Example A: Rectangular pulse

It can be shown that a rectangular pulse can be described by the following formula:

$$\sin(x) + \sin(3x)/3 + \sin(5x)/5 + \sin(7x)/7 + \dots + \dots$$

If we start with 3 summands, only, we will get a very bad approximation. (see figure 25 )

If we use more summands we'll get a better result. (see figure 26).

### Example B: Sawtooth oscillation

A sawtooth oscillation can be described in the following way:

$$\sin(x) - \sin(2x)/2 + \sin(3x)/3 - \sin(4x)/4 + - + \dots$$

If we start with a few summands only, we'll get a bad approximation.

The reader is encouraged to improve the result by adding more summands (see figure 27 ).

### Example C: One-way-rectification

It can be shown that the following formula describes a one-way-rectification :

$$1/\pi + \sin(x)/2 - 2/\pi * (\cos(2x)/3 + \cos(4x)/15 + \cos(6x)/35 + \cos(8x)/63 + + \dots)$$

The one-way-rectification is shown in figure 28.

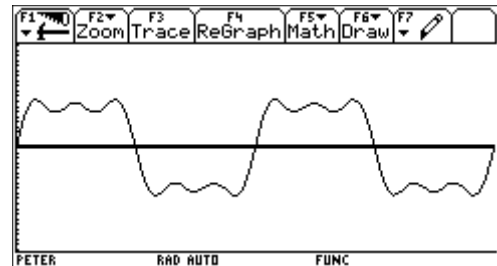


Figure 25

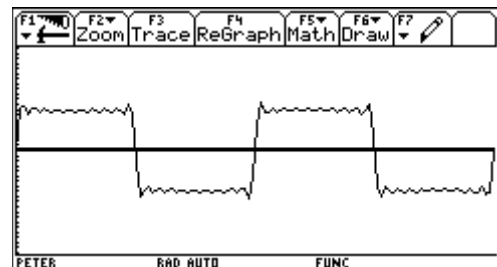


Figure 26

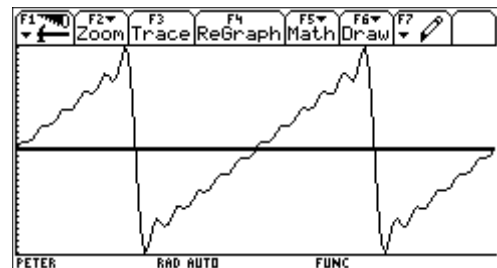


Figure 27

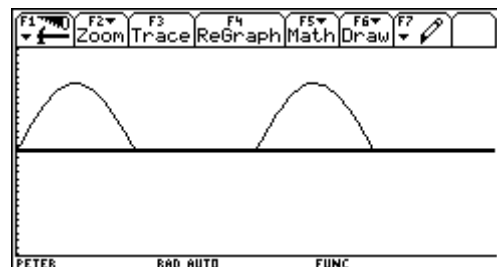


Figure 28